Exercise 2: Lake Phyto- and Zooplankton Model

ETH Zurich Course 701-0426-00L: Modelling Aquatic Ecosystems (Schuwirth)

March 6, 2024

Goals:

- Understand the process table notation introduced in section 4.1 of the manuscript.
- Understand the formulation of biogeochemical and ecological process rates introduced in section 4.2.
- Increase your familiarity with the R package ecosim.
- Understand the behaviour of the solutions of the lake phyto- and zooplankton model described in section 11.2 under constant and seasonally varying environmental conditions.

Task 1: Model with constant driving forces

Study the implementation of the model described in section 11.2 for constant driving forces. Run the model implementation below and interpret the behavior of the solutions.

```
# Model with constant driving forces
# load required packages:
if ( !require("deSolve") ) {install.packages("deSolve"); library("deSolve") }
if ( !require("ecosim") ) {install.packages("ecosim"); library("ecosim") }
# definition of model parameters:
param
       <- list(k.gro.ALG = 0.5,
                                     # 1/d
               k.gro.Z00 = 0.4,
                                     # m3/qDM/d
               k.death.ALG = 0.1,
                                    # 1/d
               k.death.Z00 = 0.05,
                                     # 1/d
               K.HPO4
                        = 0.002,
                                     # qP/m3
               Y.ZOO
                          = 0.2.
                                     # qDM/qDM
               alpha.P.ALG = 0.003,
                                     # qP/qDM
                          = 5e+006,
                                     # m2
               Α
                          = 5,
                                     # m
               h.epi
               Q.in
                          = 5,
                                      # m3/s
                                     # qP/m3
               C.HP04.in = 0.04,
               C.HP04.ini = 0.04,
                                     # gP/m3
               C.ALG.ini = 0.1,
                                      # gDM/m3
               C.ZOO.ini
                          = 0.1)
                                      # gDM/m3
```

a) **Complete** and run the definitions of the transformation processes describing the growth and death of Algae and Zooplankton. *Hint:* look at what we did in Exercise 1.

```
# definition of transformation processes
# growth of algae:
gro.ALG
         <- new(Class = "process",
                       = "Growth of algae",
                 name
                 rate = expression(k.gro.ALG
                                     *C.HP04/(K.HP04+C.HP04)
                                     *C.ALG).
                 stoich = list(C.ALG = expression(1),
                                                                    # qDM/qDM
                               C.HPO4 = expression(-alpha.P.ALG))) # gP/gDM
# death of algae: TO BE COMPLETED
death.ALG <- new(Class = ...,</pre>
                 name = ...,
                 rate = ...,
                 stoich = ...)
                                        # gDM/gDM
# growth of zooplankton:
gro.ZOO
         <- new(Class = "process",
                 name = "Growth of zooplankton",
                 rate = expression(k.gro.Z00
                                     *C.ALG
                                     *C.ZOO),
                 stoich = list(C.ZOO = expression(1),
                                                                   # qDM/qDM
                               C.ALG = expression(-1/Y.Z00)) \qquad \# gP/gDM
# death of zooplankton: TO BE COMPLETED
death.ZOO <- new(Class = ...,</pre>
                 name = ...,
                 rate = ...,
                 stoich = ...)
                                         # gDM/gDM
```

b) Complete and run the definition of the epilimnion. *Hint:* look at what we did in Exercise 1.

definition of reactor to describe the epilimnion of the lake: TO BE COMPLETED

```
epilimnion <-
 new(Class
                      = ...,
     name
                      = ...,
     volume.ini
                      = ...,
     conc.pervol.ini = list(C.HP04 = ...,
                                             # gP/m3
                                             # gDM/m3
                             C.ALG = \ldots,
                                              # gDM/m3
                             C.ZOO = ...),
      inflow
                      = ...,
                                               # m3/d
                      = list(C.HP04 = expression(C.HP04.in),
      inflow.conc
                             C.ALG = 0,
                             C.ZOO = 0),
     outflow
                      = ...,
                      = list(...))
     processes
```

c) Perform and plot the simulation of the system. Interpret the results.

```
# perform simulation:
res.11.2.a <- calcres(system.11.2.a)</pre>
# plot results with default options:
plotres(res.11.2.a)
# variables in a vector 'c()' are plotted in the same graph
plotres(res=res.11.2.a, colnames=c("C.ALG", "C.HP04", "C.ZO0"))
# variables in a list 'list()' are plotted in different graphs
plotres(res=res.11.2.a, colnames=list("C.ALG", "C.HPO4", "C.ZOO"))
# combination of the two
plotres(res=res.11.2.a, colnames=list("C.HP04", c("C.ALG", "C.ZOO")))
# plot and save as pdf
plotres(<mark>res</mark>
               = res.11.2.a,
        colnames = list("C.HP04",c("C.ALG", "C.Z00")),
        file = "exercise_2_results_a.pdf",
        width = 10,
        height = 5)
```

Task 2: Model with seasonally varying driving forces

Study the implementation of the model extension to seasonally varying driving forces. First, run the model implementation below.

```
# Model with seasonally varying driving forces
# ------
# copy the previous system definition:
system.11.2.b <- system.11.2.a</pre>
```

```
# extend model parameters:
param <- c(param,</pre>
                (beta.ALG = 0.08, # 1/aeg
= 20. # degC
           list(beta.ALG = 0.046, # 1/degC
                                      # 1/deqC
                K.I
                          = 30,
                                      # W/m2
                lambda.1 = 0.10,
                                     # 1/m
                lambda.2 = 0.10, # m2/gDM
                t.max = 230,
                                      # d
                                      # W/m2
                IO.min
                          = 25,
                IO.max
                          = 225,
                                      # W/m2
                T.min
                          = 5,
                                      # degC
                T.max
                           = 25))
                                       # deqC
# extend growth of algae and zooplankton by considering environmental factors:
gro.ALG.ext <-
  new(Class = "process",
      name = "Growth of algae extended",
      rate = expression(k.gro.ALG
                          *exp(beta.ALG*(T-T0))
                          *C.HP04/(K.HP04+C.HP04)
                          *log((K.I+I0)
                               /(K.I+IO*exp(-(lambda.1+lambda.2*C.ALG)*h.epi)))
                           /((lambda.1+lambda.2*C.ALG)*h.epi)
                          *C.ALG),
      stoich = list(C.ALG = 1,
                                                          # qDM/qDM
                    C.HPO4 = expression(-alpha.P.ALG)))
                                                          # gP/gDM
gro.ZOO.ext <-
            new(Class = "process",
                name = "Growth of zooplankton",
                rate = expression(k.gro.ZOO
                                   *exp(beta.Z00*(T-T0))
                                   *C.ALG
                                   *C.ZOO),
                stoich = list(C.ZOO = expression(1),
                                                                # qDM/qDM
                             C.ALG = expression(-1/Y.Z00)) \qquad # gP/gDM
# re-define processes in the reactor "epilimnion":
epilimnion@processes <- list(gro.ALG.ext,death.ALG,gro.ZOO.ext,death.ZOO)</pre>
# make environmental conditions (light and temperature) time dependent:
epilimnion@cond <- list(I0 = expression(0.5*(I0.min+I0.max)+</pre>
                                        0.5*(I0.max-I0.min)*
                                        cos(2*pi/365.25*(t-t.max))),
                                                                      # W/m2
                       T = \exp (0.5*(T.min+T.max))+
                                        0.5*(T.max-T.min)*
                                        cos(2*pi/365.25*(t-t.max)))) # degC
```

```
# plot the environmental conditions
t \leftarrow seq(1,2*365) \# for two years
IO <- numeric(0)</pre>
T <- numeric(0)
for(i in 1:length(t))
{
  IO[i] <- eval(epilimnion@cond$I0, envir=c(param, t=t[i]))</pre>
 T[i] <- eval(epilimnion@cond$T, envir=c(param, t=t[i]))</pre>
}
par(mfrow=c(1,2),xaxs="i",yaxs="i",mar=c(4.5,4.5,2,1.5)+0.1)
plot(t, I0, type="1")
plot(t, T, type="l")
# re-define the reactor "epilimnion" in the system definition:
system.11.2.b@reactors <- list(epilimnion)</pre>
# increase algal growth rate to compensate for new limitations:
param$k.gro.ALG <- 0.8
# replace parameters in the system definition:
system.11.2.b@param <- param</pre>
```

Second, redo the simulations and plot and interpret the behavior of the solutions.

We compare the two simulations.

Task 3: Sensitivity analysi for constant driving forces

Fill in the missing terms and perform a sensitivity analysis of the model results to the parameters

 $C_{in,HPO^{2-}}, Q_{in}, k_{gro,ALG}, k_{death,ALG}, k_{gro,ZOO}, k_{death,ZOO}, and Y_{ZOO}$

by modifying their values by factors of 2 and 1/2 for the model under constant driving forces using the function calcsens. Interpret the results. *Hint:* look at the solution of the Task 5 of Exercise 1.

Task 4 - Homework: Sensitivity analyis for seasonally varying driving forces

Do a sensitivity analysis for seasonally varying driving forces and discuss the differences to the case with constant driving forces.

TO BE COMPLETED

Theory questions

- 1. Are the algae concentrations controlled bottom-up (by phosphate limitation) or top-down (by grazing of zooplankton)?
- 2. What is the reason for oscillating concentrations under constant driving forces? What happens when you introduce periodic driving forces?
- 3. What are the main deficits of the model compared to a real lake?
- 4. What is your expectation regarding the response of the model to the change in each parameter, does the result match your expectation and can you explain the observed changes?